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Method of and scaling unit for scaling a three-dimensional model

The invention relates to a method of scaling a three-dimensional input model in a three-dimensional input space into a three-dimensional output model which fits in a predetermined three-dimensional output space.

The invention further relates to a scaling unit for scaling a three-dimensional input model in a three-dimensional input space into a three-dimensional output model which fits in a predetermined three-dimensional output space.

The invention further relates to an image display apparatus comprising:

- receiving means for receiving a signal representing a three-dimensional model;
- a scaling unit as described above; and

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 rendering means for rendering a three-dimensional image on basis of the threedimensional output model.

The invention further each relates to a computer program product to be loaded by a computer arrangement, comprising instructions to scale a three-dimensional input model in a three-dimensional input space into a three-dimensional output model which fits in a predetermined three-dimensional output space.

The probability that the size of a three-dimensional scene does not match with the display capabilities of an image display device, on which the scene is to be displayed, is high, e.g. the dimensions of a three-dimensional scene comprising a house are much bigger than typical dimensions of a display device. Hence, a scaling operation is required. Other reasons why scaling might be required is to adapt the geometry of the three-dimensional model representing the three-dimensional scene to a transmission channel or to adapt the three-dimensional model to the viewer's preferences.

Linear scaling operations on a three-dimensional model representing a three-dimensional scene are well known. Scaling of depth information is in principle performed by means of a linear adaptation of the depth information related to the depth range of the output space. Alternatively, information which exceeds the limits of the display capabilities are clipped.

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A disadvantage of depth adaptation or scaling is that it might result in reduction of depth impression. Especially the linear depth scaling might be disadvantageous for the depth impression of the scaled three-dimensional model because the available depth range of display devices is often relatively small.

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It is an object of the invention to provide a method of the kind described in the opening paragraph which results in a scaled three-dimensional output model with a relatively strong three-dimensional impression.

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This object of the invention is achieved in that a first input surface in the three-dimensional input space, having a first distance to a viewpoint, is projected to a first output surface in the predetermined three-dimensional output space by applying a first scaling factor and whereby a second input surface in the three-dimensional input space, having a second distance to the viewpoint, which is smaller than the first distance, is projected to a second output surface in the predetermined three-dimensional space, by applying a second scaling factor which is larger than the first scaling factor. In other words, the applied scaling factor is not constant but is related to the distance between an input surface and a viewpoint. A smaller distance means a larger scaling factor. An advantage of the method according to the invention is that the three-dimensional input model is adapted, i.e. reshaped, such that the depth impression is at least maintained or even enhanced. Notice that with a linear three-dimensional scaling, the depth impression is reduced if the depth range of the predetermined three-dimensional output space is much smaller than the depth of the three-dimensional input space. With the method according to the invention this reduction is prevented. Optionally the depth impression is even enhanced.

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In an embodiment of the method according to the invention, a first input data point of the three-dimensional input model, being located at the first input surface is projected to a first output data point of the three-dimensional output model, being located at the first output surface by means of a perspective projection relative to the viewpoint, and a second input data point of the three-dimensional input model, being located at the second input surface is projected to a second output data point of the three-dimensional output model, being located at the first output surface by means of a perspective projection relative to the viewpoint. In other words, the input data points are projected to respective data output points on basis of a single viewpoint. An advantage of this embodiment of the method according to the invention, is that the original depth impression of the input three-

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dimensional model is maintained. That means that the original depth impression and the depth impression of the output three-dimensional model are substantially mutually equal.

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In another embodiment of the method according to the invention, a first input data point of the three-dimensional input model, being located at the first input surface is projected to a first output data point of the three-dimensional output model, being located at the first output surface by means of a perspective projection relative to the viewpoint, and a second input data point of the three-dimensional input model, being located at the second input surface is projected to a second output data point of the three-dimensional output model, being located at the first output surface by means of a perspective projection relative to a further viewpoint. In other words, the input data points are projected to respective data output points on basis of multiple viewpoints. An advantage of this embodiment of the method according to the invention, is that the original depth impression of the input three-dimensional model is enhanced. That means that the depth impression of the input three-dimensional model is even higher than the original depth impression of the input three-dimensional model.

It is a further object of the invention to provide a scaling unit of the kind described in the opening paragraph which is arranged to provide a scaled three-dimensional output model with a relatively strong three-dimensional impression.

This object of the invention is achieved in that the scaling unit comprises computing means for computing coordinates of output data points of the three-dimensional output model corresponding to respective input data points of the three-dimensional input model, whereby a first one of the input data points which is located at a first input surface in the three-dimensional input space, having a first distance to a viewpoint, is projected to a first one of the output data points which is located at a first output surface in the predetermined three-dimensional output space by applying a first scaling factor and whereby a second one of the input data points which is located at a second input surface in the three-dimensional input space, having a second distance to the viewpoint, which is smaller than the first distance, is projected to a second one of the output data points which is located at a second output surface in the predetermined three-dimensional space, by applying a second scaling factor which is larger than the first scaling factor.

It is a further object of the invention to provide an image processing apparatus of the kind described in the opening paragraph which is arranged to provide a scaled three-dimensional output model with a relatively strong three-dimensional impression.

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This object of the invention is achieved in that the scaling unit comprises computing means for computing coordinates of output data points of the three-dimensional output model corresponding to respective input data points of the three-dimensional input model, whereby a first one of the input data points which is located at a first input surface in the three-dimensional input space, having a first distance to a viewpoint, is projected to a first one of the output data points which is located at a first output surface in the predetermined three-dimensional output space by applying a first scaling factor and whereby a second one of the input data points which is located at a second input surface in the three-dimensional input space, having a second distance to the viewpoint, which is smaller than the first distance, is projected to a second one of the output data points which is located at a second output surface in the predetermined three-dimensional space, by applying a second scaling factor which is larger than the first scaling factor.

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It is a further object of the invention to provide a computer program product of the kind described in the opening paragraph which results in a scaled three-dimensional output model with a relatively strong three-dimensional impression.

This object of the invention is achieved in the computer program product, after being loaded in a computer arrangement comprising processing means and a memory, provides said processing means with the capability to compute coordinates of output data points of the three-dimensional output model corresponding to respective input data points of the three-dimensional input model, whereby a first one of the input data points which is located at a first input surface in the three-dimensional input space, having a first distance to a viewpoint, is projected to a first one of the output data points which is located at a first output surface in the predetermined three-dimensional output space by applying a first scaling factor and whereby a second one of the input data points which is located at a second input surface in the three-dimensional input space, having a second distance to the viewpoint, which is smaller than the first distance, is projected to a second one of the output data points which is located at a second output surface in the predetermined three-dimensional space, by applying a second scaling factor which is larger than the first scaling factor.

Modifications of the scaling unit and variations thereof may correspond to modifications and variations thereof of the image processing apparatus, the method and the computer program product, being described.

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These and other aspects of the method, of the scaling unit, of the image processing apparatus, and of the computer program product according to the invention will become apparent from and will be elucidated with respect to the implementations and embodiments described hereinafter and with reference to the accompanying drawings, wherein:

Fig. 1 schematically shows a method of scaling according to the prior art;

Fig. 2A schematically shows a first embodiment of the method of scaling according to the invention;

Fig. 2B schematically shows a second embodiment of the method of scaling according to the invention;

Fig. 3 schematically shows the mapping of input data points into data elements of a memory device; and

Fig. 4 schematically shows an image processing apparatus according to the invention.

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There are several types of models for the storage of three-dimensional information, i.e. a three-dimensional model:

- Wireframes, e.g. as specified for VRML. These models comprise a structure of lines and faces.
 - Volumetric data-structures or voxel maps (Voxel means volume element). These volumetric data-structures comprise a three-dimensional array of elements. Each element has three dimensions and represents a value of a property. E.g. CT (Computer tomography) data is stored as a volumetric data-structure in which each element corresponds to a respective Hounsfield value (unit to express the amount of X-ray absorption).
 - Two-dimensional image with depth map, e.g. a two-dimensional image with RGBZ values. This means that each pixel comprises three color component values and a depth value. The three color component values also represent a luminance value.
- Image based models, e.g. stereo image pairs or multiview images. These types of images are also called light fields.

Conversions of data represented by one type of three-dimensional model into another three-dimensional model is possible. E.g. data represented with a wireframe or a two-

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dimensional image with depth map can be converted by means of rendering into data represented with a volumetric data-structure or image based model.

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The amount of depth which can be realized with a three-dimensional display device depends on its type. With a volumetric display device the amount of depth is fully determined by the dimensions of the display device. Stereo displays with e.g. glasses have a soft limit for the amount of depth which depends on the observer. Observers might become fatigued if the amount of depth is too much caused by a "conflict" between lens accommodation and mutual eye convergence. Autostereoscopic display devices, e.g. based on an LCD with a lenticular screen for multiple views, have a theoretical maximum depthrange which is determined by the amount of views.

Fig. 1 schematically shows a method of linear scaling according to the prior art. Fig. 1 shows a three-dimensional input model 100 and a linear scaled three-dimensional output model 102 which fits in a predetermined three-dimensional output space 104, e.g. corresponding to the viewing range of a three-dimensional display device. The scaling means that each of the input data points I_1, I_2, I_3 and I_4 is transformed to a respective one of the output data points O_1 , O_2 , O_3 and O_4 . E.g. in Fig. 1 is depicted that input data point I_1 , which is located on the first input surface 106 at the border of the three-dimensional input model 100, is mapped to output data point O_1 , which is located on the first output surface 110 at the border of the predetermined three-dimensional output space 104. In Fig. 1 is also depicted that input data point I_3 , which is located at the second input surface 108 at an other border of the three-dimensional input model 100, is mapped to output data point O_3 , which is located at the second output surface 112 at the other border of the predetermined three-dimensional output space 104. Both the three-dimensional input model 100 and the three-dimensional output model 102 have a block shape. E.g. the width $W_i(z3)$ of a first side, located at the first input surface 106 (z = z3) of the three-dimensional input model 100 is equal to the width $W_i(z2)$ of a second side, located at the second input surface 108 (z = z2) of the threedimensional input model 100 and the width $W_o(z4)$ of a first side (z = z4), located at the first output surface 110 of the three-dimensional output model 102 is equal to the width $W_a(z)$ of a second side (z = z1), located at the second output surface 112 of the three-dimensional output model 102.

Fig. 2A schematically shows the method of scaling according to the invention. Fig. 2A shows a three-dimensional input model 100 and a three-dimensional output model

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200 scaled in perspective of a single viewpoint V_1 . Although the three-dimensional input model 100 has a rectangular shape, the three-dimensional output model 200 has a trapezoid shape. E.g. the first width $W_i(z3)$ of the first side (z=z3) of the three-dimensional input model 100 is equal to the second width $W_i(z2)$ of the second side (z=z2) of the three-dimensional input model 100 but the first width $W_o(z4)$ of the first side (z=z4) of the three-dimensional output model 200 is different from the second width $W_o(z1)$ of the second side of the three-dimensional output model 200. In other words, the change of the first width $W_i(z3)$ and second width $W_i(z2)$ of the three-dimensional input model 100 into the first width $W_o(z4)$ and second width $W_o(z1)$, respectively, depends on the location of the different sides of the three-dimensional input model 100, i.e. the z-coordinates.

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The scaling, i.e. transformation of the three-dimensional input model 100 into the predetermined three-dimensional output space 104 is such that each of the output data points O_1 , O_2 , O_3 and O_4 is disposed at or located very close to (depending on the accuracy of computation) respective lines from the respective input data points I_1 , I_2 , I_3 and I_4 to a single viewpoint V_1 . E.g. a first one O_3 of the output data points is located on a first line l_1 from the first input data point I_3 to the viewpoint V_1 and also a second one O_2 of the output data points is located on a second line l_2 from the second input data point I_2 to the particular viewpoint V_1 .

As said above, the scaling according to the invention is a kind of perspective projection resulting in a deformation of the three-dimensional input model. Below some computations are provided to show the extent of the deformation. The extent of deformation is related to the difference in the change of a first side and the change of a second side.

The first width $W_o(z4) = ||O_2 - O_1||$ of the first side of the three-dimensional output model 200 in which the output data points O_1 and O_2 are located, can be computed with Equation 1:

$$W_o(z4) = \frac{W_i(z3)}{z3}(z1+d), \qquad (1)$$

with $W_i(z3) = ||I_2 - I_1||$ the first width of the first side of the three-dimensional input model 100, in which the input data points I_1 and I_2 are located, z1 the z-coordinate of the border of the predetermined three-dimensional output space 104, z3 the z-coordinate of the first

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surface of the three-dimensional input model 100 and d the depth, i.e. z-range of the predetermined three-dimensional output space 104.

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The second width $W_{\nu}(z1) = ||O_4 - O_3||$ of the second side of the three-dimensional output model 200 in which the output data points O_3 and O_4 are located, can be computed with Equation 2:

$$W_o(z1) = \frac{W_i(z2)}{z^2} z1,$$
 (2)

with $W_I(z2) = ||I_4 - I_3||$ the second width of the second side of the three-dimensional input model 100 in which the input data points I_3 and I_4 are located and z2 the z-coordinate of the second side of the three-dimensional input model 100.

The difference in size between the two output sides can be computed with Equation 3.

$$D = W_o(z1) - W_o(z4) = \frac{W_i(z2)}{z2} z1 - \frac{W_i(z3)}{z3} (z1 + d)$$
 (3)

The relative difference between the two output sides corresponds with the difference in scaling factors being applied for the different sides, i.e. surfaces. See Equation 4.

$$D_{rel} = \frac{W_o(z1) - W_o(z4)}{W(z1)} * 100\%$$
 (4)

In Table 1 some examples are listed. Example 1. Suppose the three-dimensional model 100 corresponds to a scene, e.g. a room of 5m*5m*10m, i.e. $W_i(z2) = 5m$, $W_i(z3) = 5m$ and z3 - z2 = 5m. The predetermined three-dimensional output space 104 corresponds to a volumetric display device with a depth range of 10cm, i.e. d = 0.10m. The distance between the viewpoint V_1 , where the observer 106 is located, and the volumetric display device is equal to 2 m, i.e. z1=2m. Then the first width $W_o(z4)$ of the first side of the scaled three-dimensional output model 200 is equal to 0.7m and the second width $W_o(z1)$ of the second side of the scaled three-dimensional output model 200 is equal to 1m. Hence, the difference between the two output sides is equal to 0.3m and the difference in scaling factors is 30%.

Example 2. Most of the values of Example 1 are applicable. However now the three-dimensional model 100 corresponds to a long corridor of 5m*20m. Then the first width $W_o(z4)$ of the first side of the scaled three-dimensional output model 200 is equal to 0.35m while the second width $W_o(z1)$ of the second side of the scaled three-dimensional output

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model 200 is still equal to 1m. Hence, the difference between the two output sides is equal to 0.65m and the difference in scaling factors is 65%.

Example 3. At z = z3 a first actor is located having a width $W_i(z3)$ of 0.5m and at z = z2 a second actor is located having a width $W_i(z2)$ of 0.5m. The distance between the two actors is 1m, i.e. z3 - z2 = 1. The representation of the first actor is scaled to the first output surface 110 of the scaled three-dimensional output model 200. The width $W_o(z4)$ which is equal to 0.1m The representation of the second actor is scaled to the second output surface 112. The width $W_o(z1)$ is equal to 0.095m. Hence, the difference between the two output sides is equal to 0.005m and the difference in scaling factors is 5%.

Example 4. Most of the values of Example 3 are applicable. However, now the predetermined three-dimensional output space 104 corresponds to a volumetric display device with a depth range of 5cm, i.e. d = 0.05m. Hence, the difference between the two output sides is equal to 0.007m and the difference in scaling factors is 7%.

Example 5. Most of the values of Example 3 are applicable. However, now the predetermined three-dimensional output space 104 corresponds to a volumetric display device with a depth range of 5cm, i.e. d = 0.02m. Hence, the difference between the two output sides is equal to 0.008m and the difference in scaling factors is 8%.

Table 1. Examples of scaling.

Example	$W_i(z2)$	$W_i(z3)$	zl	<i>z</i> 2	z3 d	$W_o(z1)$	$W_o(z4)$	D	$D_{\it ret}$ [%]
1	5	5	2	10	150.10	1	0.7	0.3	30
2	5	5	2	10	300.10	1	0.35	0.65	65
3	0.5	0.5	2	10	110.10	0.100	0.095	0.005	5
4	0.5	0.5	2	10	110.05	0.100	0.093	0.007	7
5	0.5	0.5	2	10	110.02	0.100	0.092	0.008	8

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Fig. 2B schematically shows a second embodiment of the method of scaling according to the invention. In this embodiment there is not a single viewpoint but there is a range of viewpoints V_1 , V_2 . The scaling, i.e. transformation of the three-dimensional input model 100 into the predetermined three-dimensional output space 104 is such that each of the output data points O_1 , O_2 , O_3 and O_4 is disposed at or located very close to (depending on the accuracy of computation) respective lines from the respective input data points

 I_1, I_2, I_3 and I_4 to a range of viewpoints V_1, V_2 . E.g. a first one O_3 of the output data points is located on a first line I_1 from the first input data point I_3 to the viewpoint V_1 but a second one O_2 of the output data points is located on a second line I_2 from the second input data point I_2 to the another viewpoint V_2 . Preferably, each of the input surfaces of the three-dimensional input model is projected into a corresponding output surface of the three-dimensional output model on basis of its own viewpoint. When comparing the three-dimensional output model 202 as depicted in Fig. 2B with the three-dimensional output model 200 as depicted in Fig. 2A, it can be observed that the deformation of the three-dimensional input model 100 is more in the embodiment of the method according to the invention as described in connection with Fig. 2B than in the embodiment of the method according to the invention as described in connection with Fig. 2A. Notice that $W_0^*(z4) < W_0(z4)$. The extent of the additional deformation is related to the amount of enhancement of the depth impression.

It will be clear that instead of enhancement of the depth impression, as described in connection with Fig. 2B also a limited reduction of depth impression can be achieved by applying multiple viewpoints, e.g. one viewpoint behind or above the other. This is not depicted.

Fig. 3 schematically shows the mapping of input data points $I_1 - I_{11}$ into data cells 304-320 of a memory device 302. The memory device 302 comprises a three-dimensional data structure. This three-dimensional data structure represents the predetermined three-dimensional output space. From the three-dimensional data structure only one z, x-slice, i.e. y-coordinate is constant, is depicted in Fig. 3. The different y, x-slices 330-340, i.e. z-coordinate constant, might correspond to the different viewing planes of a volumetric display device. The values, e.g. color and luminance, of the different output data points $O_1 - O_{13}$ are stored in the respective data cells 304-320 of the memory device 302. For each input data point $I_1 - I_{11}$ the corresponding data cell is determined and filled with the appropriate color and luminance value. E.g. input data point I_1 is mapped into output data point O_1 and stored into data cell 312 and input data point I_1 is mapped into output data point O_2 and stored into data cell 304. The mapping from input data points to output data points is based on the known coordinates of the input data points, the predetermined three-dimensional output space and the viewpoint V_1 . The x, y and z coordinates of the output data points can be determined with Equation 5,6 and 7, respectively.

$$O_i(x) = f_x(I_i(x, y, z))$$
(5)

$$O_i(y) = f_y(I_i(x, y, z))$$
(6)

$$O_i(z) = f_*(I_i(x, y, z))$$
 (7)

In this case, the z-coordinates of the output data points $O_1 - O_6$ are computed as follows. It is known, that there are six input data points $I_1 - I_6$ located on one line I_1 , through the viewpoint V_1 . The z-coordinate of the first output surface, which is located at a border of the predetermined three-dimensional output space is known a priori. The z-coordinate of the first output data point O_1 on the line I_1 is set to this known z-coordinate. The z-coordinate of the second output surface, which is located at the other border of the predetermined three-dimensional output space is known a priori. The z-coordinate of the last output data point O_6 on the line I_1 is set to this latter z-coordinate. The other z-i dividing the z-range of the predetermined three-dimensional output space into five equidistant distances. It should be noted that alternative mappings are possible, see e.g. below. A prerequisite is that the order of input data points is not changed.

Alternatively, the values of output data points O_7 - O_{10} are computed on basis of distances between input data points I_7 - I_{10} . In this case, the z-coordinates of the output data points O_7 - O_{10} are computed as follows. It is known, that there are four input data points I_7 - I_{10} located on one line I_2 , through the viewpoint V_1 . The z-coordinate of the first output surface, which is located at a border of the predetermined three-dimensional output space is known a priory. The z-coordinate of the first output data point O_7 on the line I_2 is set to this known z-coordinate. The z-coordinate of the second output surface, which is located at the other border of the predetermined three-dimensional output space is also known a priori. The z-coordinate of the last output data point O_{10} on the line I_2 is set to this latter z-coordinate. The z-coordinates output data points O_8 and O_9 are computed on basis of distances between input data points I_7 - I_{10} and the distance between the first output surface and the second output surface. Optionally, further values of output data points O_{11} - O_{12} are computed on basis of interpolation of multiple input data points, e.g. I_7 - I_{10} .

In a further alternative, the value of a particular output data point O_{13} is computed on basis of other output data points, e.g. because the corresponding input data point I_{11} belongs to an object in the three-dimensional input model. In Fig. 3 it is depicted

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that the three input data points I_5 , I_9 and I_{11} are on one line I_4 , indicating that they belong to one object. The particular input data point I_{11} is located on the line I_3 through the viewpoint V_1 . Because there are no other input data points on the line I_3 , it is arbitrary in which data cell, i.e. to which z-coordinate the output data point O_{13} is mapped. It might be stored in the data cell of a first y, x-slice 330 corresponding to the first surface of the three-dimensional output model or in a last y, x-slice 340 corresponding to the second surface of the three-dimensional output model. An other option is depicted in Fig. 3. The z-coordinate of the output data point O_{13} is based on the z-coordinates of the output data points O_5 and O_9 .

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It should be noted that the storage scheme as described above is just an example. Alternatively, the three-dimensional output model is not stored in such a rigid three-dimensional data structure having fixed planes, i.e. y, x-slice 330. An option is to store from each output data point not only a luminance and/or color value but also its coordinates.

Fig. 4 schematically shows an image processing apparatus 400 according to the invention. The image processing apparatus 400 comprises:

- a receiving unit 402 for receiving a signal representing a three-dimensional input model;
 - a scaling unit 404 for scaling the three-dimensional input model into a three-dimensional output model; and
 - rendering means 405 for rendering a three-dimensional image on basis of the threedimensional output model.

The signal is provided at the input connector 410. The signal e.g. is a digital stream of data which is according to the VRML specification. The signal may be a broadcast signal received via an antenna or cable but may also be a signal from a storage device like a VCR (Video Cassette Recorder) or Digital Versatile Disk (DVD).

The scaling unit 404 comprises computing means 407 for computing coordinates of output data points of the three-dimensional output model corresponding to respective input data points of the three-dimensional input model, whereby a first one of the input data points which is located at a first input surface in the three-dimensional input space, having a first distance to a viewpoint, is projected to a first one of the output data points which is located at a first output surface in the predetermined three-dimensional output space by applying a first scaling factor and whereby a second one of the input data points which is located at a second input surface in the three-dimensional input space, having a second distance to the viewpoint, which is smaller than the first distance, is projected to a second one of the output data points which is located at a second output surface in the predetermined

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three-dimensional space, by applying a second scaling factor which is larger than the first scaling factor. The computation of coordinates of output data points is as described in connection with Fig. 2A, Fig. 2B and Fig. 3.

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The computing means 407 of the scaling unit 404 and the rendering means 405 may be implemented using one processor. This is not depicted as such. Normally, these functions are performed under control of a software program product. During execution, normally the software program product is loaded into a memory, like a RAM, and executed from there. The program may be loaded from a background memory, like a ROM, hard disk, or magnetically and/or optical storage, or may be loaded via a network like Internet.

Optionally an application specific integrated circuit provides the disclosed functionality.

The image processing apparatus optionally comprises a display device 406 for displaying the output images of the rendering means. The image processing apparatus 400 might e.g. be a TV. Alternatively the image processing apparatus 400 does not comprise the optional display device but provides the output images to an apparatus that does comprise a display device 406. Then the image processing apparatus 400 might be a set top box, a satellite-tuner, a VCR player, a DVD player or recorder and the like. Optionally the image processing apparatus 400 comprises storage means, like a hard-disk or means for storage on removable media, e.g. optical disks. The image processing apparatus 400 might also be a system being applied by a film-studio or broadcaster. An other option is that the image processing apparatus 400 is comprised in a game device, for playing games.

It should be noted that the viewpoints which are used to project the input data points to the output data points, do not necessarily have to match with an actual position of an observer. Besides that, the viewpoints which are used to project the input data points to the output data points do not necessarily have to match with another viewpoint which is used to render a three-dimensional image. That means data the different viewpoints should be interpreted as central points for projection. These viewpoints define the geometrical relation between input data points and output data points.

It should be noted that the above-mentioned embodiments illustrate rather than limit the invention and that those skilled in the art will be able to design alternative embodiments without departing from the scope of the appended claims. In the claims, any reference signs placed between parentheses shall not be constructed as limiting the claim. The word 'comprising' does not exclude the presence of elements or steps not listed in a claim. The word "a" or "an" preceding an element does not exclude the presence of a plurality of such elements. The invention can be implemented by means of hardware

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comprising several distinct elements and by means of a suitable programmed computer. In the unit claims enumerating several means, several of these means can be embodied by one and the same item of hardware. The usage of the words first, second and third, etcetera do not indicate any ordering. These words are to be interpreted as names.